

7.3 Trigonometric Equations

Solve $2 \sin \theta + \sqrt{3} = 0$, $0 \leq \theta < 2\pi$.

$$2 \sin \theta = -\sqrt{3}$$

$$\sin \theta = -\frac{\sqrt{3}}{2}$$

$$\theta = \frac{4\pi}{3}, \frac{5\pi}{3}$$

Solve $\tan(\theta - \frac{\pi}{2}) = 1$, $0 \leq \theta < 2\pi$

$$\theta - \frac{\pi}{2} = \frac{\pi}{4}$$

$$\theta - \frac{\pi}{2} = \frac{5\pi}{4}$$

$$\theta = \frac{3\pi}{4}$$

$$\theta = \frac{7\pi}{4}$$

Solve $\sin(2\theta) = \frac{1}{2}$, $0 \leq \theta < 2\pi$.

$$2\theta = \frac{\pi}{6} + 2\pi \quad 2\theta = \frac{5\pi}{6} + 2\pi$$

$$\theta = \frac{\pi}{12} + \pi \quad \theta = \frac{5\pi}{12} + \pi$$

$$\theta = \frac{\pi}{12}, \frac{5\pi}{12}, \frac{13\pi}{12}, \frac{17\pi}{12}$$

Solve $4 \cos^2 \theta = 1$, $0 \leq \theta < 2\pi$.

$$\cos^2 \theta = \frac{1}{4}$$

$$\cos \theta = \sqrt{\frac{1}{4}}$$

$$\cos \theta = \pm \frac{1}{2}$$

$$\theta = \frac{\pi}{3}, \frac{2\pi}{3}, \frac{4\pi}{3}, \frac{5\pi}{3}$$

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