

$$y = \sin x$$

$$y = a \sin(\underbrace{bx - c}_{\text{period}}) + d$$

↑
horizontal shift

$$P = \frac{2\pi}{b}$$

$$bx - c = 0$$

$$bx - c = 2\pi$$

$$\#1 \ y = \sin 4\theta$$

$$4x = 0$$

$$x = 0$$

$$4x = 2\pi$$

$$x = \frac{\pi}{2}$$

$$(0, 0) \left(\frac{\pi}{8}, 1\right) \left(\frac{\pi}{4}, 0\right) \left(\frac{3\pi}{8}, -1\right) \left(\frac{\pi}{2}, 0\right)$$

$$\#5 \quad y = \sin \left(x + \frac{5\pi}{6} \right)$$

$$x + \frac{5\pi}{6} = 0$$

$$x = -\frac{5\pi}{6}$$

$$x + \frac{5\pi}{6} = 2\pi$$

$$x = \frac{7\pi}{6}$$

$$\frac{12\pi}{6} - \frac{5\pi}{6}$$

$$\left(-\frac{5\pi}{6}, 0 \right) \left(-\frac{\pi}{3}, 1 \right) \left(\frac{\pi}{6}, 0 \right) \left(\frac{2\pi}{3}, -1 \right) \left(\frac{7\pi}{6}, 0 \right)$$

$\frac{-2\pi}{6}$
 $\frac{4\pi}{6}$

$$\#10 \quad y = \sin\left(3x - \frac{3\pi}{4}\right)$$

$$\frac{8\pi}{4} + \frac{3\pi}{4}$$

$$3x - \frac{3\pi}{4} = 0$$

$$3x = \frac{3\pi}{4}$$

$$x = \frac{\pi}{4}$$

$$\frac{3\pi}{12}$$

$$3x - \frac{3\pi}{4} = 2\pi$$

$$3x = \frac{11\pi}{4}$$

$$x = \frac{11\pi}{12}$$

$$\left(\frac{\pi}{4}, 0\right) \left(\frac{5\pi}{12}, 1\right) \left(\frac{\pi}{12}, 0\right) \left(\frac{3\pi}{4}, -1\right) \left(\frac{11\pi}{12}, 0\right)$$

$$\frac{9\pi}{12}$$