

5-1

Midsegments of Triangles

Content Standards

G.CO.10 Prove theorems about triangles . . . the segment joining the midpoints of two sides of a triangle is parallel to the third side and half the length . . .
Also G.CO.12 and G.SRT.5

Objective To use properties of midsegments to solve problems

A **midsegment of a triangle** is a segment connecting the midpoints of two sides of the triangle.

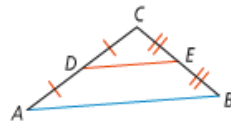
Take note

Theorem 5-1 Triangle Midsegment Theorem

Theorem

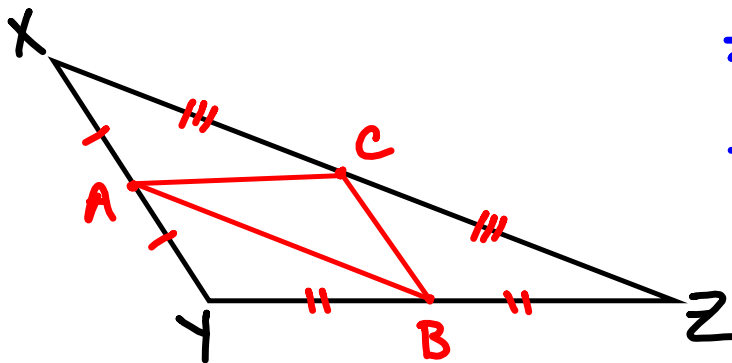
If a segment joins the midpoints of two sides of a triangle, then the segment is parallel to the third side and is half as long.

If . . .
D is the midpoint of \overline{CA} and
E is the midpoint of \overline{CB}



Then . . .
 $\overline{DE} \parallel \overline{AB}$ and
 $DE = \frac{1}{2}AB$

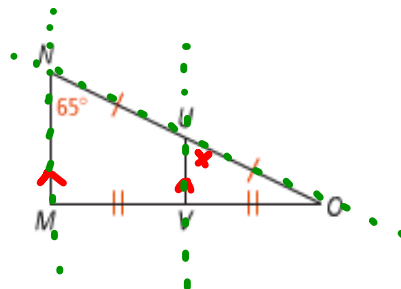
You will prove Theorem 5-1 in Lesson 6-9.



$$\begin{aligned} \overline{AB} &\parallel \overline{XZ} & AB &= \frac{1}{2}XZ \\ \overline{BC} &\parallel \overline{XY} & BC &= \frac{1}{2}XY \\ \overline{AC} &\parallel \overline{YZ} & AC &= \frac{1}{2}YZ \end{aligned}$$

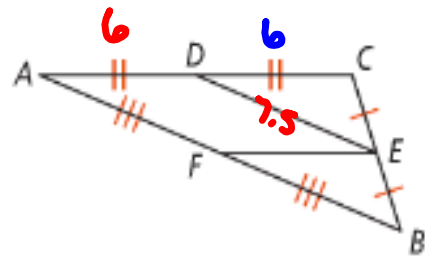
Got It? 1. a. In $\triangle XYZ$, A is the midpoint of \overline{XY} , B is the midpoint of \overline{YZ} , and C is the midpoint of \overline{XZ} . What are the three pairs of parallel segments?

b. Reasoning What is $m\angle VUO$ in the figure at the right? Explain your reasoning.



$m\angle VUO = 65^\circ$
Corresponding \angle s Thm

Got It? 2. In the figure at the right, $AD = 6$ and $DE = 7.5$.
What are the lengths of \overline{DC} , \overline{AC} , \overline{EF} , and \overline{AB} ?



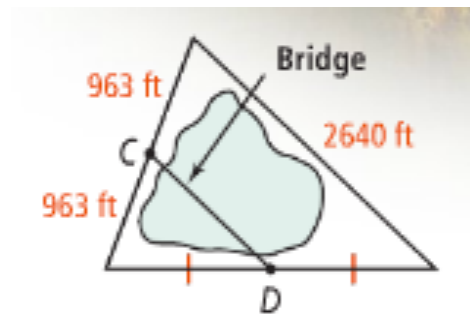
$$\overline{DC} = 6$$

$$\overline{AC} = 6 + 6 = 12$$

$$\overline{EF} = \frac{12}{2} = 6$$

$$\overline{AB} = 7.5 + 7.5 = 15$$

Got It? 3. \overline{CD} is a bridge being built over a lake, as shown in the figure at the right. What is the length of the bridge?



$$\begin{aligned}\overline{CD} &= \frac{2640}{2} \\ &= 1320 \text{ ft}\end{aligned}$$

Name

5.1

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Notes 5.2